

BERYLLIUM PARABOLIC REFRACTIVE X-RAY LENSES

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Collaboration

ESRF in Grenoble

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Wuppertal University

M. Richwin, B. Griesebock, R. Frahm

Advanced Photon Source

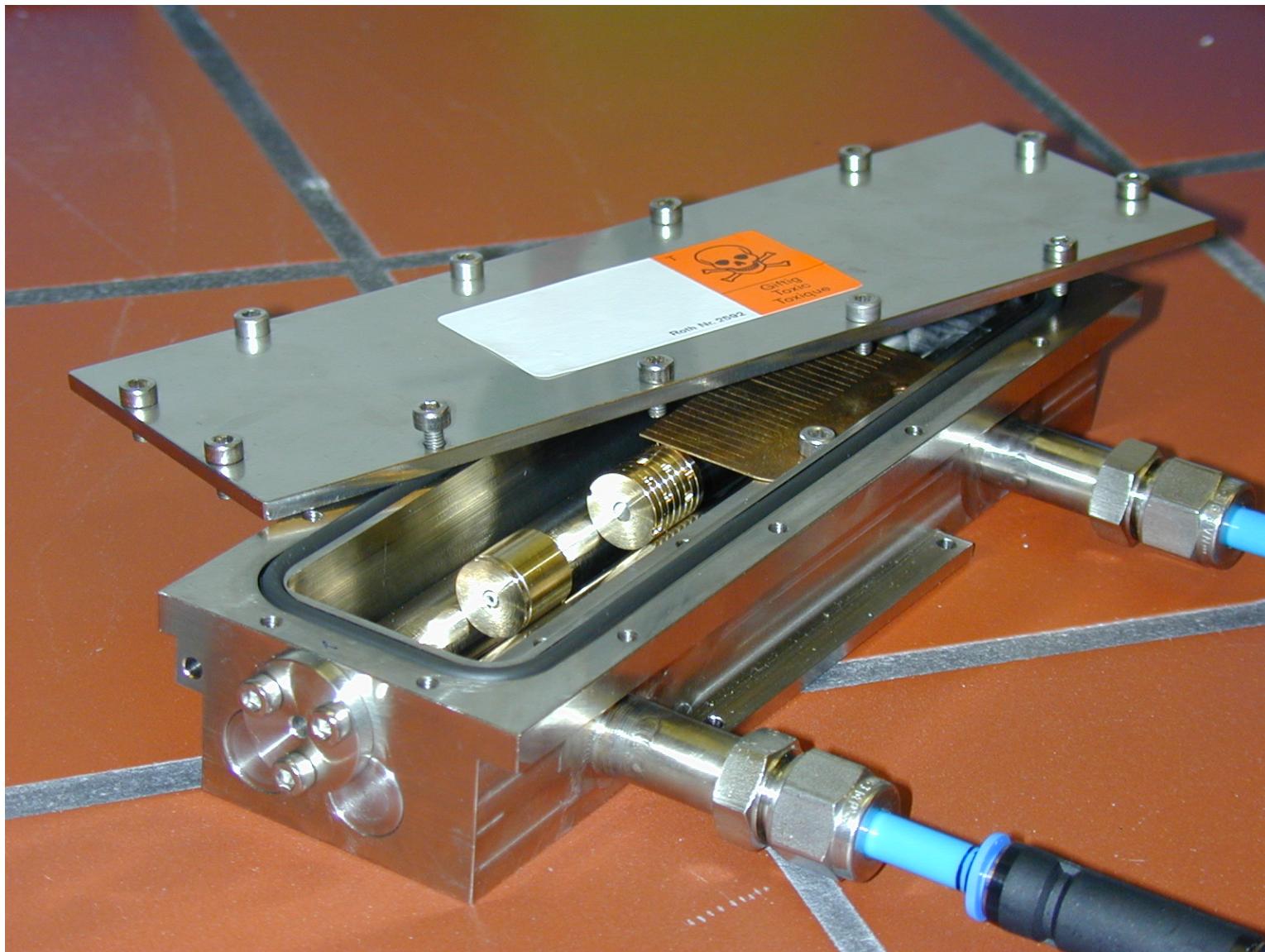
D. R. Haeffner, A. Mashayekhi

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DESY-HS

Beryllium Lenses



A. PARABOLIC REFRACTIVE X-RAY LENSES

- novel optical components for hard x-rays (6 to 120 keV)
- focuses in both directions
- **can be used like glass lenses for visible light,**
but Numerical Aperture is small ($10^{-3} \dots 10^{-4}$)
- compact and robust, easy to align and to operate
- Applications in
 - micro- and nanofocusing
 - imaging in absorption & phase contrast
 - imaging in fluorescence mode
 - microtomography
 - coherent x-ray scattering: speckle spectroscopy

The problem

index of refraction $n = 1 - \delta + i\beta$ $\delta, \beta \sim 10^{-6} > 0$

- refraction is weak
- absorption is strong $\beta = \lambda\mu/4\pi$
- focal length is long

,, There are no refractive lenses for x-rays!“ W.C.Roentgen

- focusing lens must be concave

But **refraction is not zero**

absorption is not infinite

Strategy for refractive x-ray lenses

- small radius of curvature R: $f = R / 2\delta$
- stacking of many lenses in a row: $f = R / 2N\delta$
- low Z lens material:
candidates: Be, B, C, Al, Si
- profile must be parabolic: no spherical aberration
- refractive x-ray lenses are by far less sensitive to surface roughness than mirrors are! (\Rightarrow easier to manufacture)

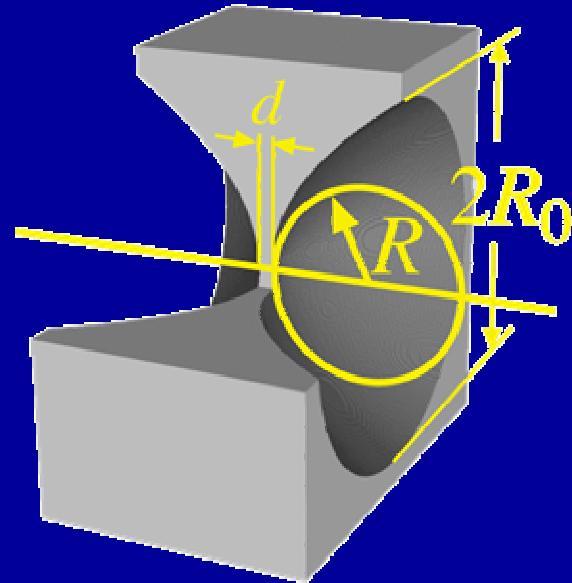
PARABOLIC REFRACTIVE X-RAY LENSES

DESIGNED & MADE AT AACHEN UNIVERSITY

Parabolic Refractive Lenses

Lens surfaces are paraboloids of rotation

single lens



parameters for Be lenses:

$$R = 200\mu\text{m}$$

$$2R_0 = 1\text{mm}$$

$$d = 50\mu\text{m}$$

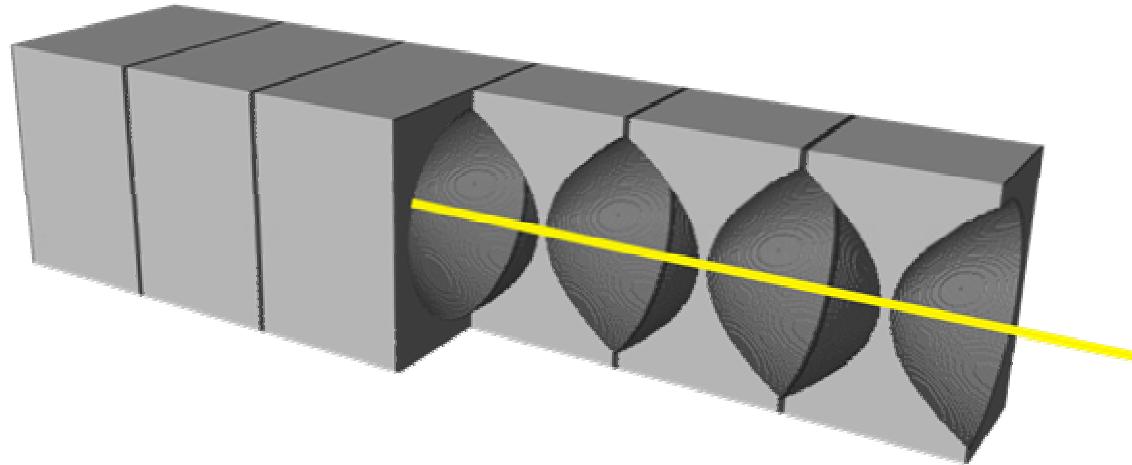
parabolic profile: no spherical aberration

focusing in full plane

=> excellent imaging optics

Parabolic Refractive Lenses

stack of lenses: $f = R / 2N\delta$ typical: 0.3m - 2m

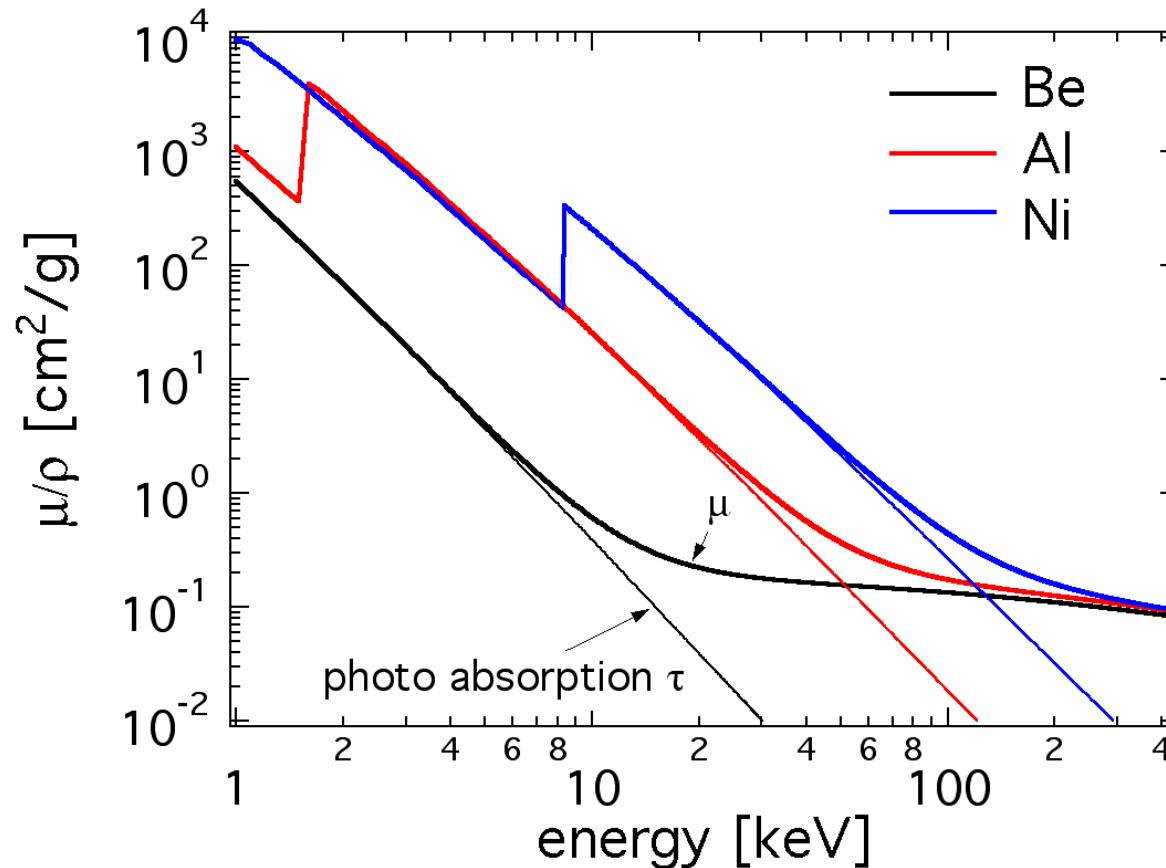


variable number of lenses : 1 to about 300

Focal distance can be adjusted to fit experimental requirements

Attenuation of X-Rays in Matter

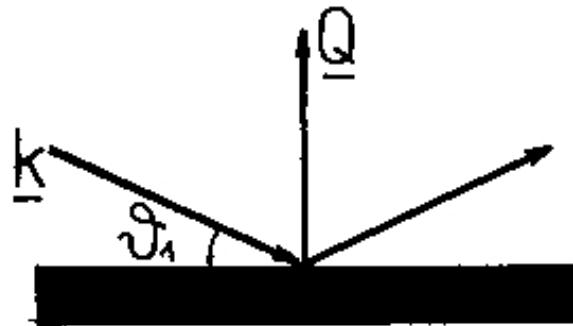
attenuation coefficient: $\mu = \tau + \mu_{\text{compton}}$



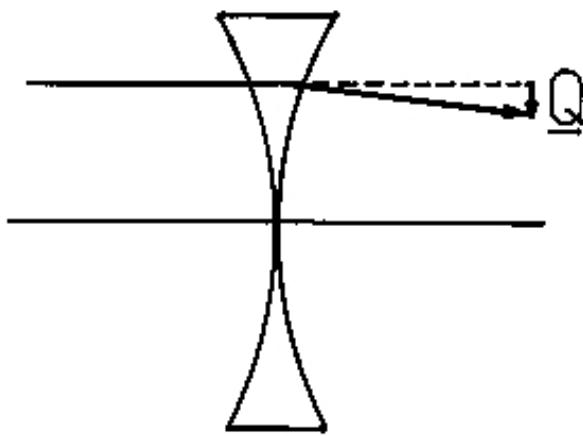
- photo absorption: $\tau \sim Z^3/E^3$
- Compton scattering dominates at high x-ray energies

Influence of surface roughness

mirror



lens



$$\text{Damping} \sim \exp[-Q^2 \sigma^2]$$

$$\text{momentum transfer } Q = 2k \sin \theta_1 = 2k \theta_1$$

$$\textbf{Mirror} \quad Q = 7 \cdot 10^{-2} \text{ A}^{-1} \qquad @ \quad \theta_1 \sim 0.3^\circ \quad \& \quad \lambda = 1\text{A}$$

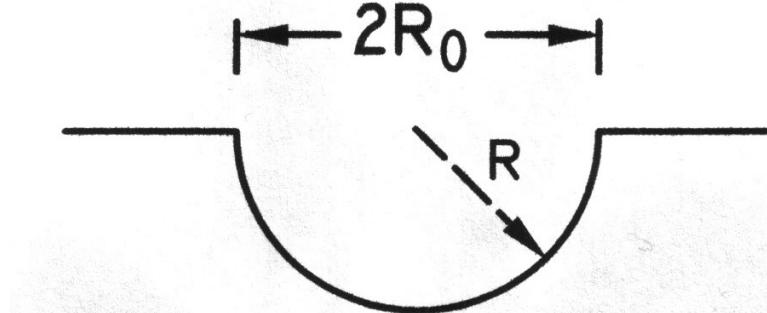
$$\textbf{lens stack} \quad Q = N^{1/2} k \delta = 1.4 \cdot 10^{-4} \text{ A}^{-1} \quad @ \quad N = 100 \quad \& \quad \lambda = 1\text{A}$$

a lens is about a factor of 500 less sensitive to surface roughness!

Parabolic Refractive Lenses

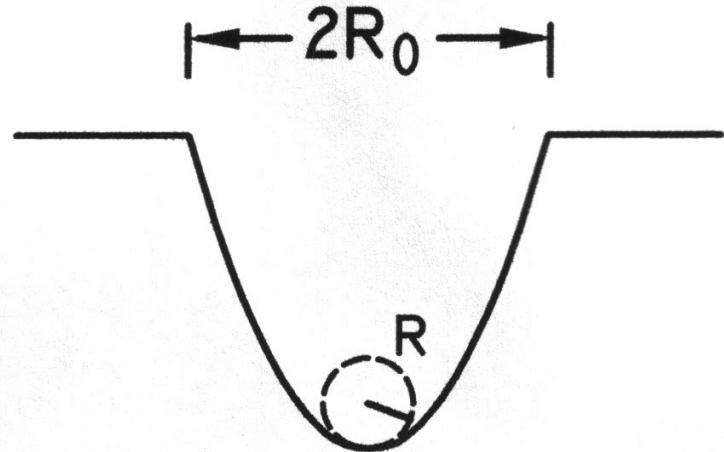
Advantage: aperture is independent of radius of curvature

spherical lens:



$$R_0 \leq R$$

parabolic lens:

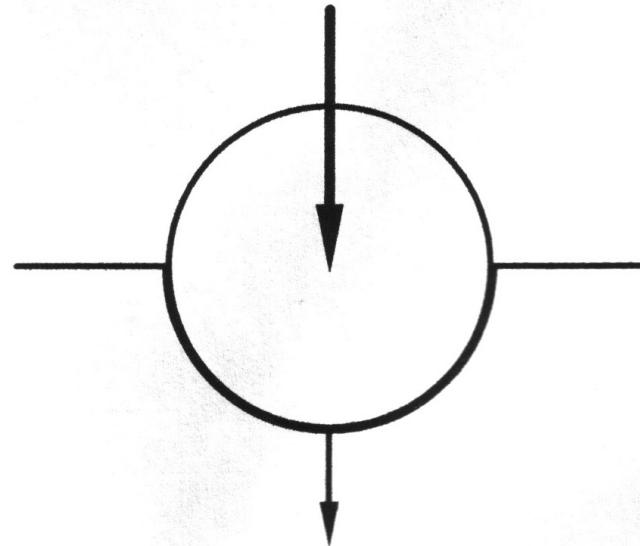


$$R_0 \text{ and } R \text{ independent}$$

Parabolic Refractive Lenses

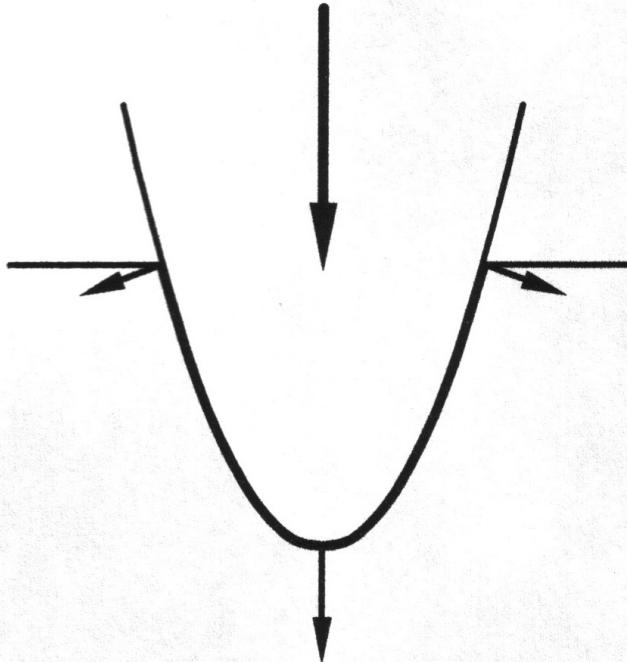
Advantage: fabrication easier than for spherical profile

spherical lens:



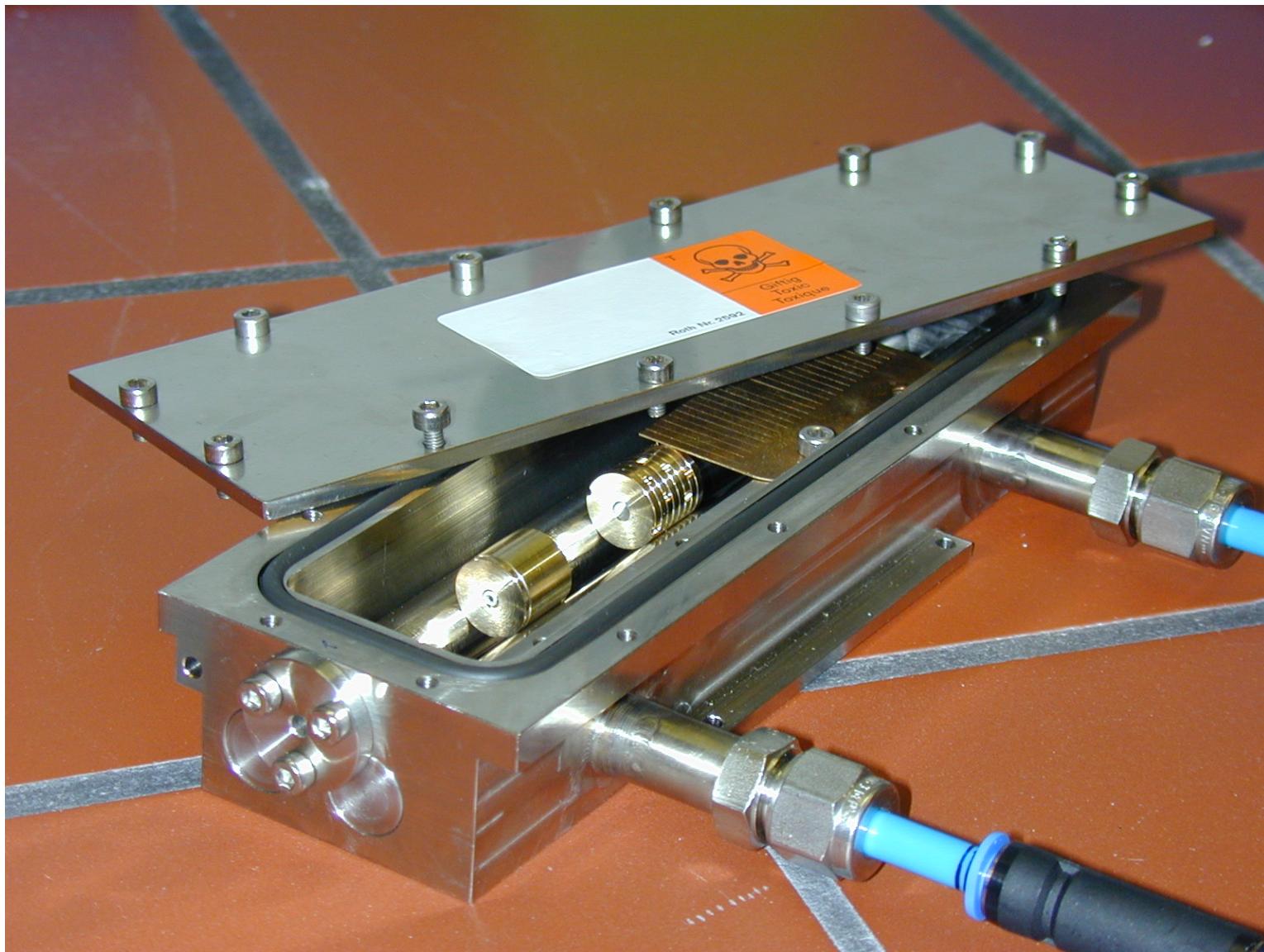
no normal force at equator

parabolic lens:



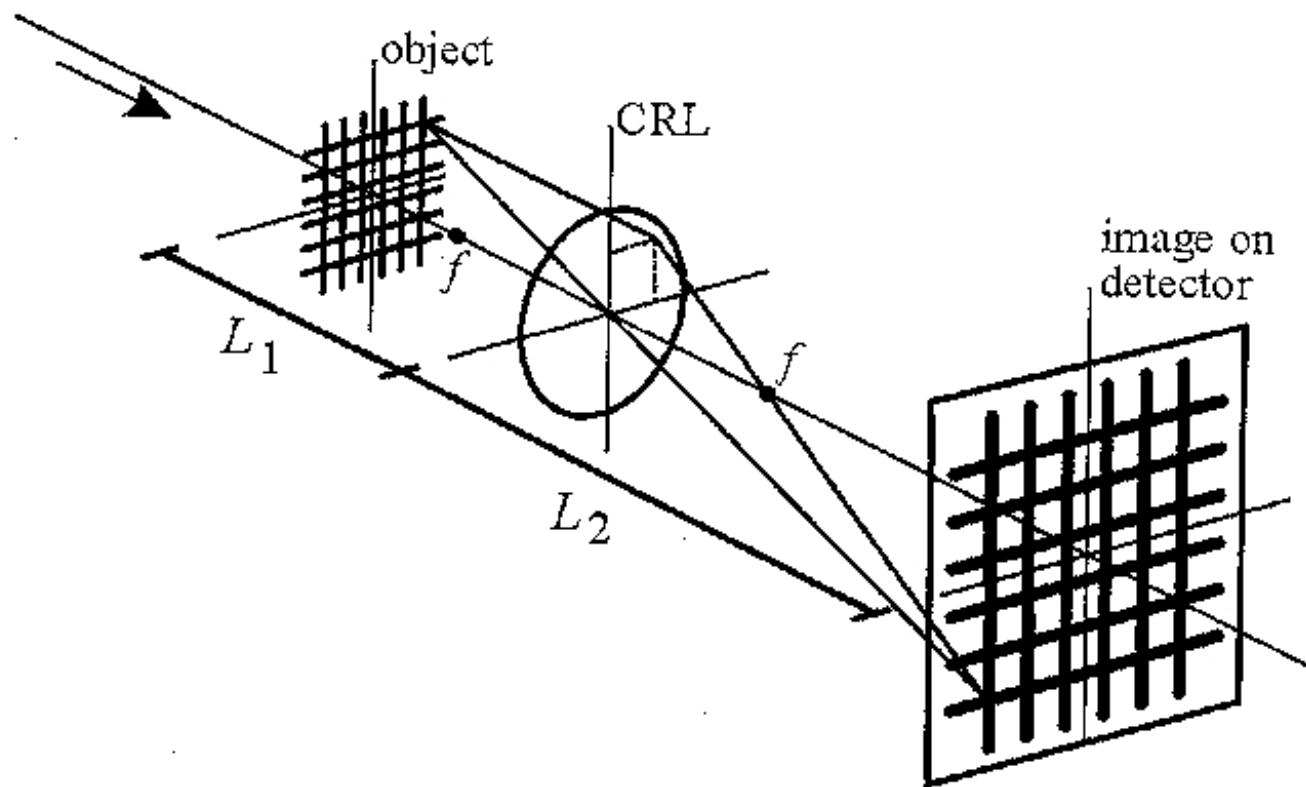
normal forces yield smooth surface

Beryllium Lenses



B. HARD X-RAY MICROSCOPY

Illumination of object by synchrotron radiation

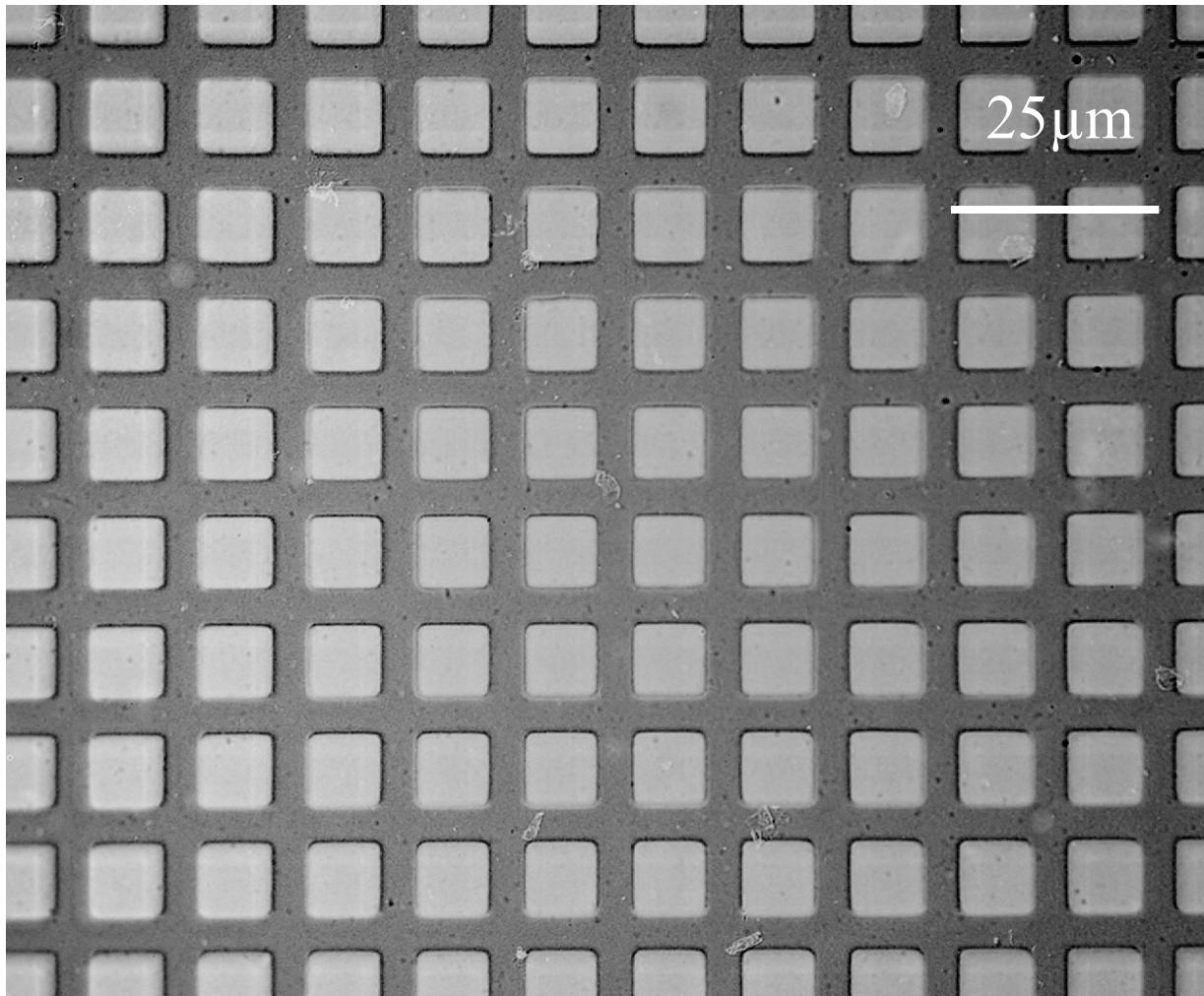


Magnified image for $L_2 \gg L_1$

$$\text{magnification } M = L_2 / L_1 \quad L_2 = L_1 f / (L_1 - f)$$

Hard X-Ray Microscopy

Ni-mesh (2000mesh) imaged by Be lens



parameters:

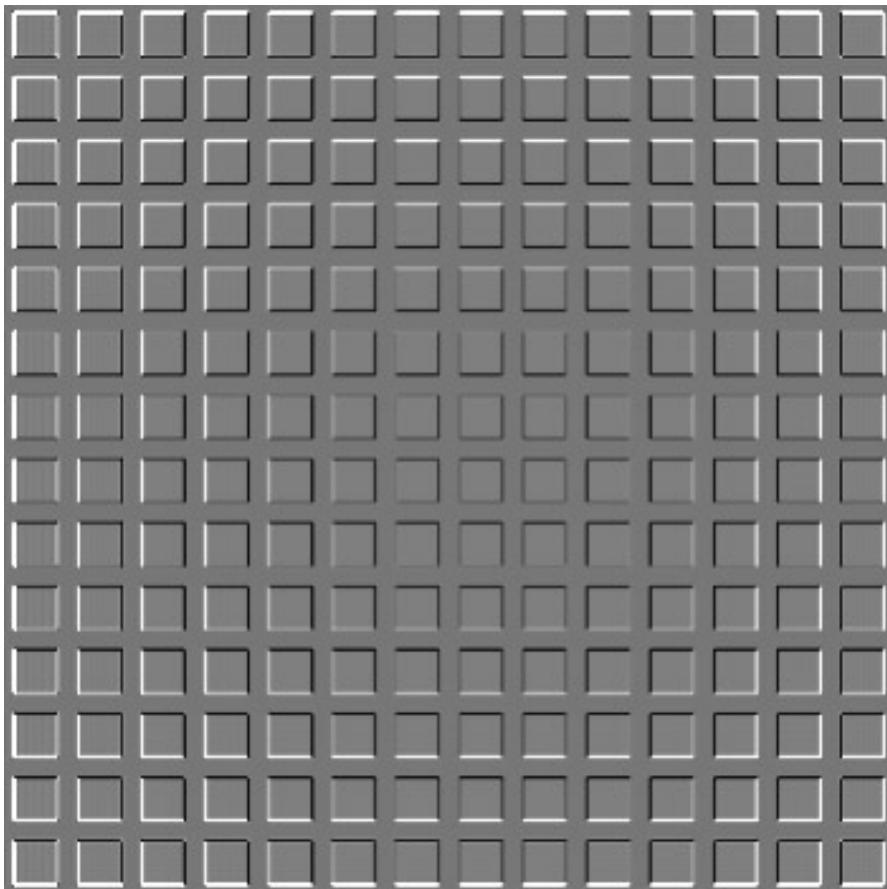
- $E = 12\text{keV}$
- $N = 91$ (Be)
- $f = 495\text{mm}$,
- $m = 10x$

Detector:

high resolution
x-ray film
(inverted contrast)

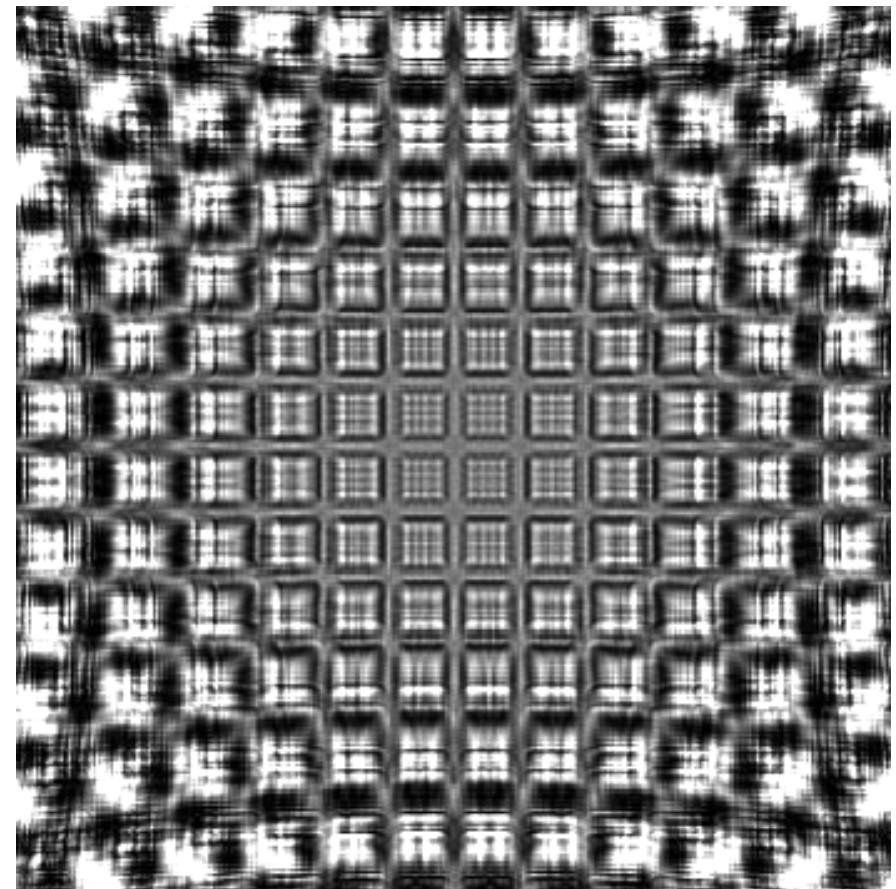
Hard X-Ray Microscopy

parabolic lenses



25μm

spherical lenses

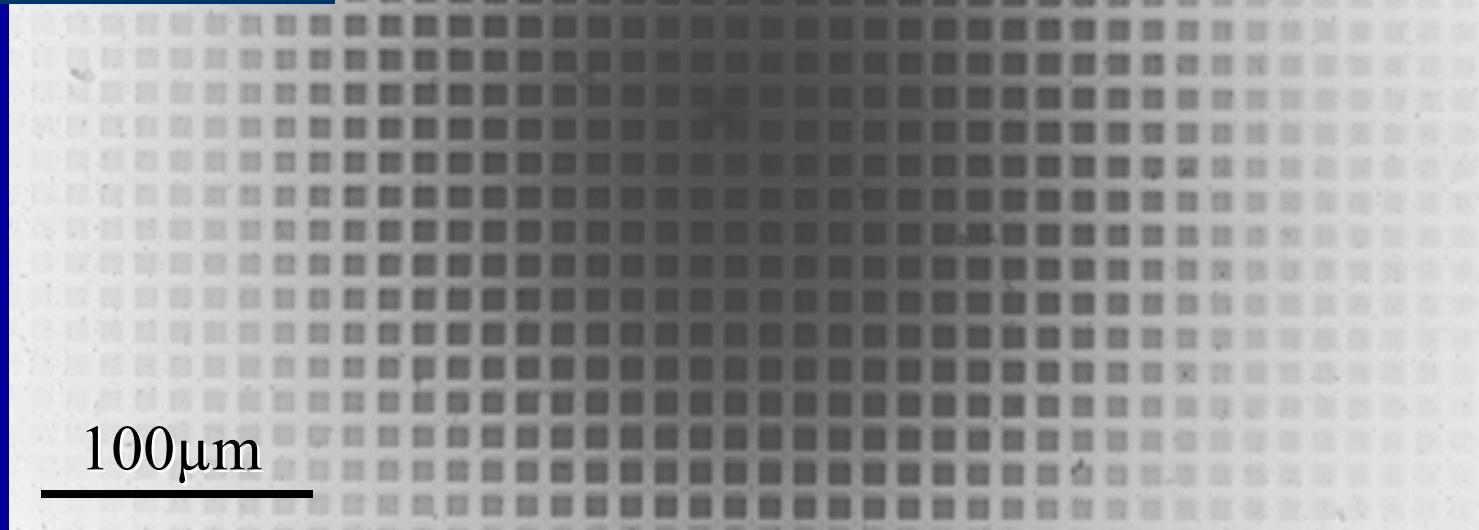
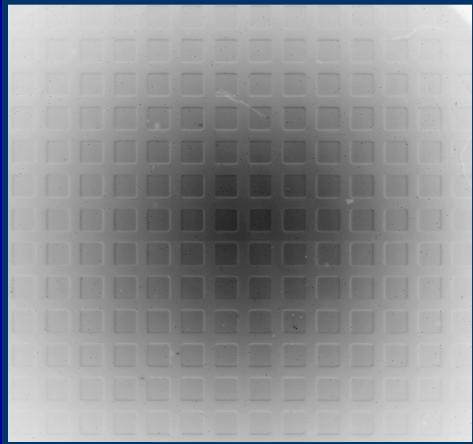


Field of View

Al: 25.5keV

($f = 1.05\text{m}$)

Be: 12keV ($N = 91, f = 495\text{mm}, m = 10x$)



Coherent Microsource

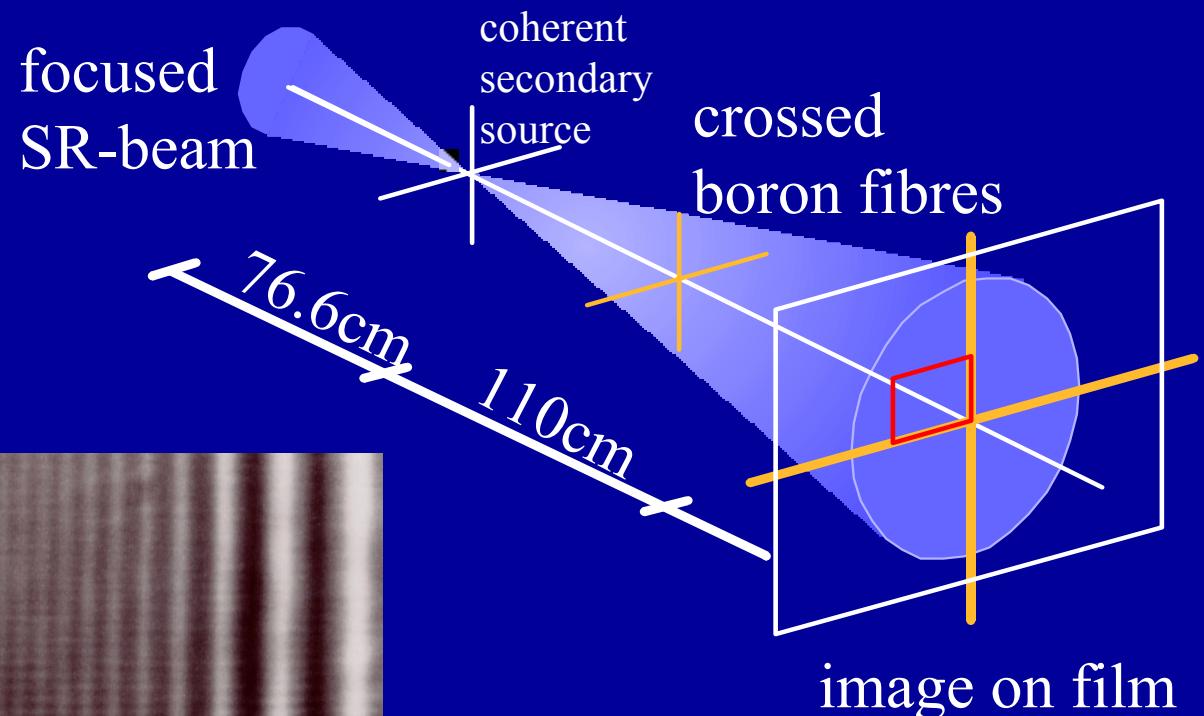
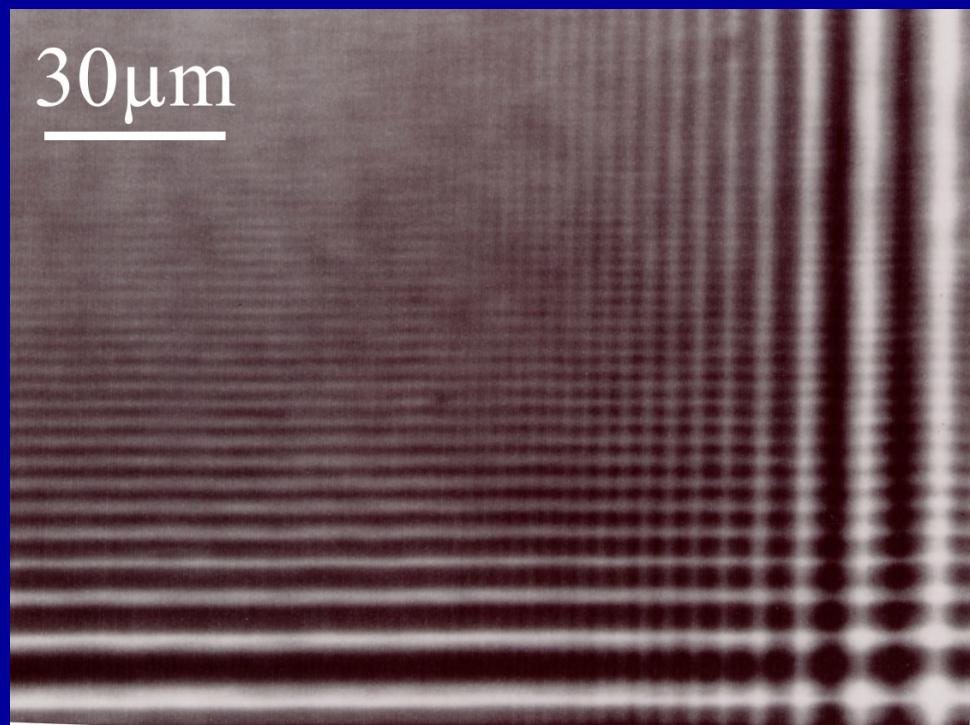
Energy: 14.4keV

CRL: $N = 50$

$f = 764\text{mm}$,

$d_{\text{lat}} = 451\text{nm}$,

spot size: $0.5\mu\text{m}$



Lateral resolution of microscope

$$d_{tr} = 0.75 \lambda / 2 \text{ N.A.} = 0.75 \lambda L_1 / D_{\text{eff}}$$

D_{eff} decreases by photoabsorption

is ultimately limited by Compton scattering

D_{eff} typically 100 to 300 μm for Al

300 to 900 μm for Be (matched to U beam size)

resolution

achieved in Al: 350 nm

in Be: 100 nm (80 nm expected for this geometry)

expected in Be : about 50 nm (present technology)

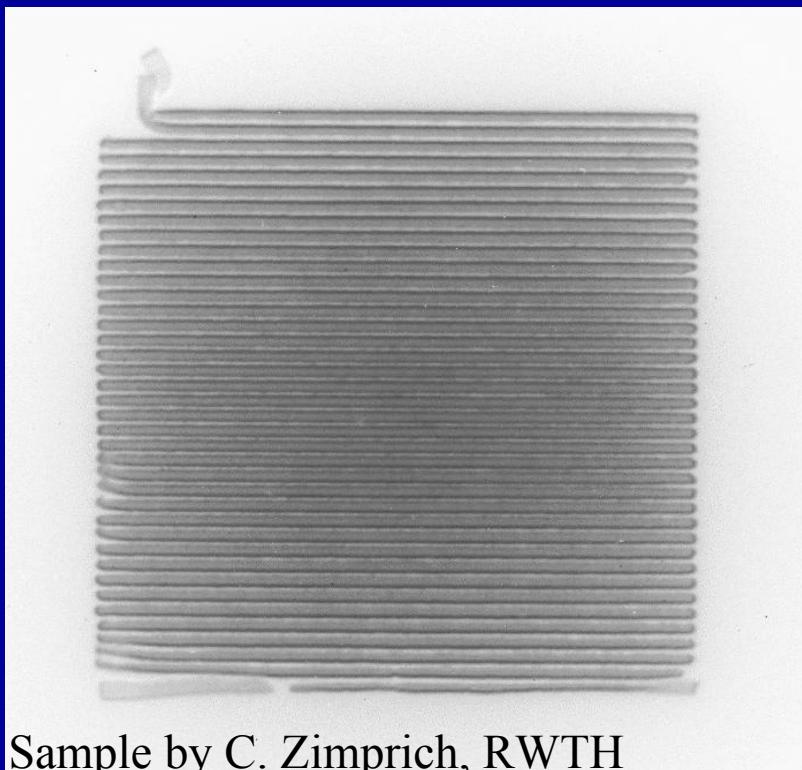
ultimately 10 to 20 nm

see poster 6.49 on nanolenses today

Hard X-Ray Microscopy

gold test structure:

- pitch: $2\mu\text{m}$
- line width: $1\mu\text{m}$
- thickness: $2\mu\text{m}$

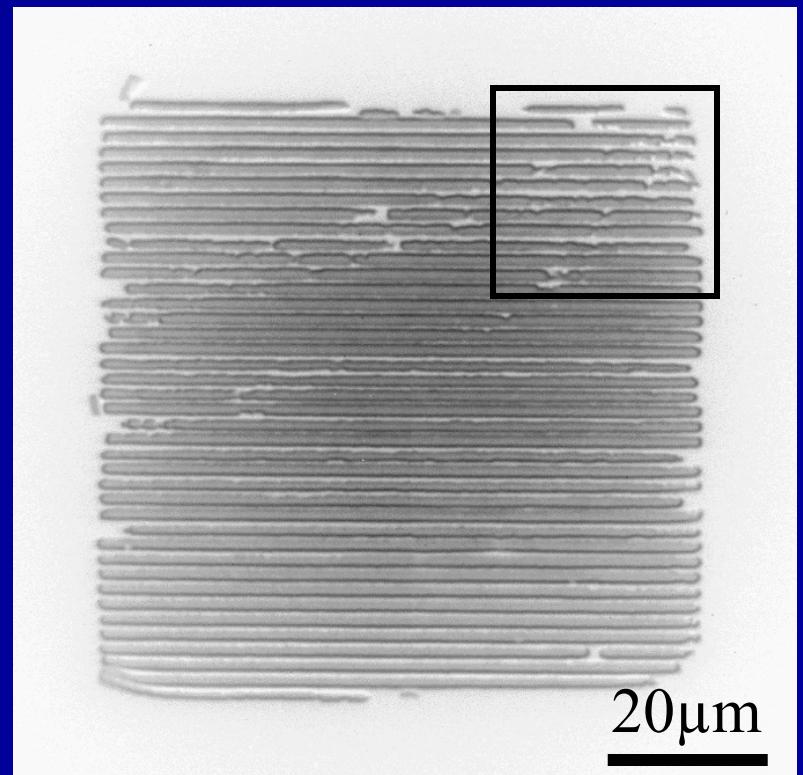


Sample by C. Zimprich, RWTH

parameters of microscope:

- $E = 25.5\text{keV}$, $N = 120$ (Al)
 $f = 1.05\text{m}$, magn.: 21x

test structure with defects



Lateral Resolution

Demonstration of resolution:
conventional projection image:



10μm

high resolution x-ray camera
(FReLoN2000, $E = 20\text{keV}$)

resolution about $0.8\mu\text{m}$

limited by

- scattering in scintillator
- resolution of visible light optics.

Lateral Resolution

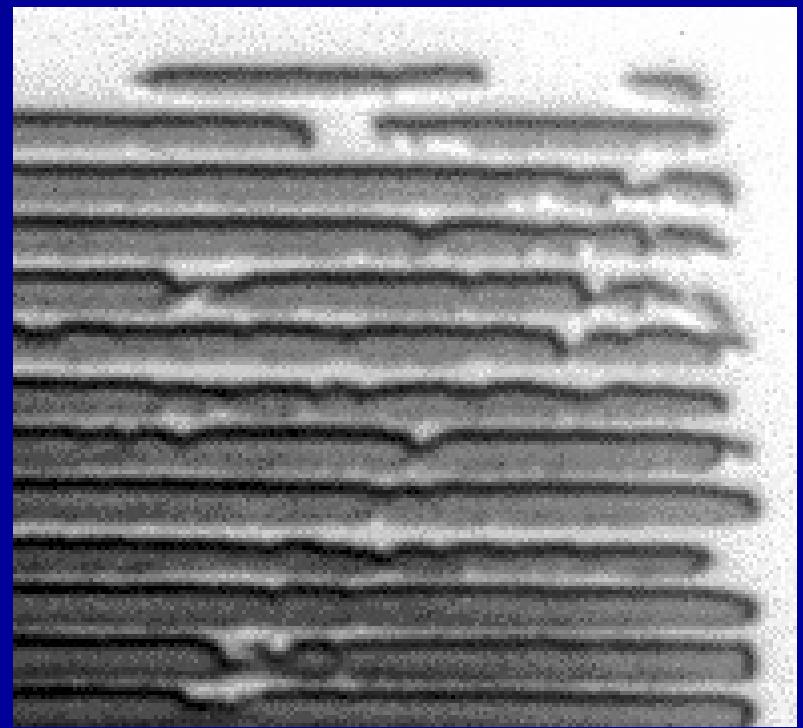
Demonstration of resolution:
conventional projection image:



10μm

high resolution x-ray camera
(FReLoN2000 , $E = 20\text{keV}$)

magnified image:



Al objective lens ($N = 120$)
($E = 25.5\text{keV}, f = 1.05\text{m}$,
 $m = 21x$)

Lateral Resolution

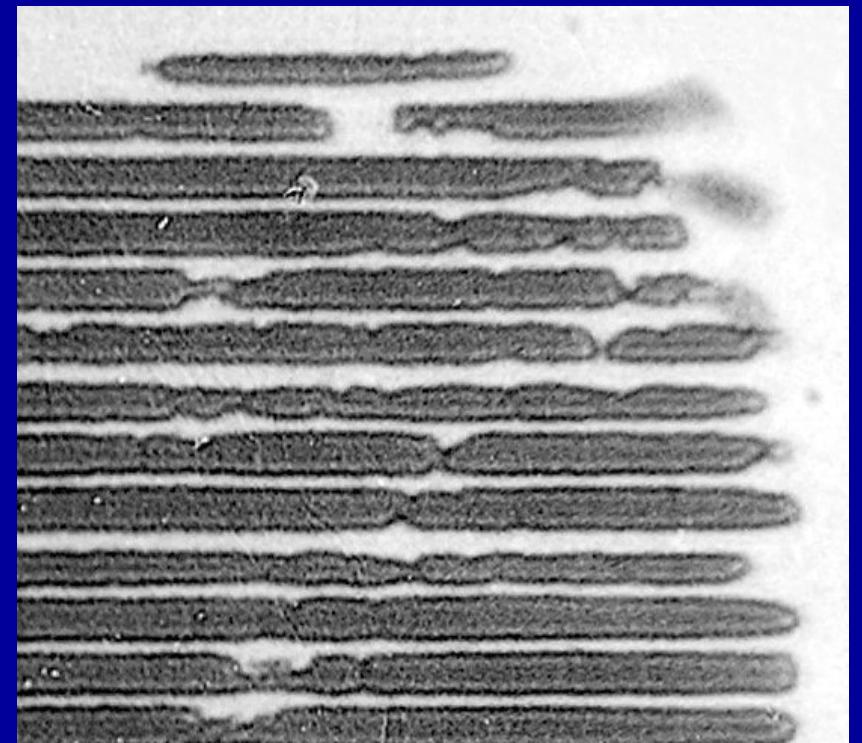
Demonstration of resolution:
conventional projection image:



$10\mu\text{m}$

high resolution x-ray camera
(FReLoN2000 , $E = 20\text{keV}$)

magnified image:

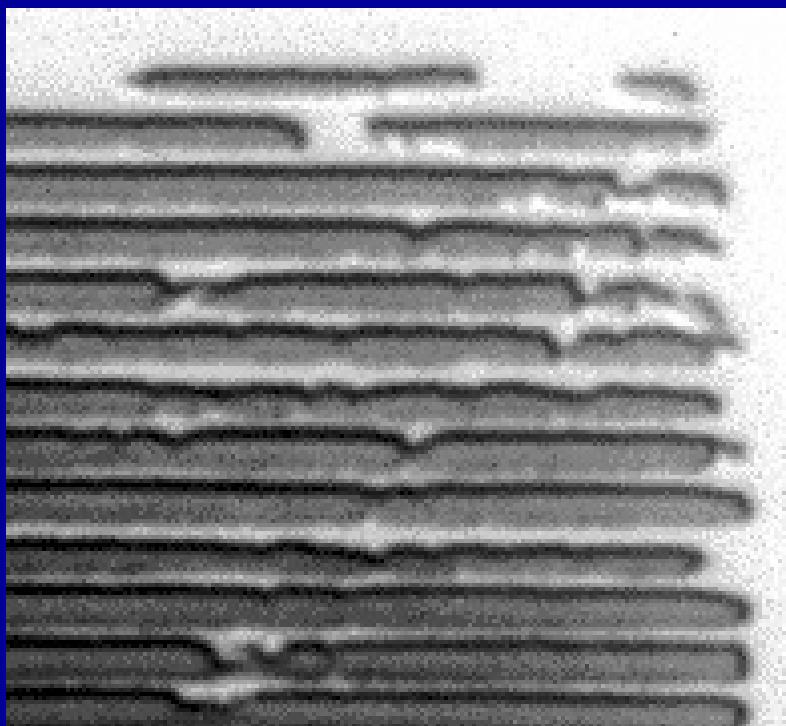


Be objective lens ($N = 91$)

$(E = 12\text{keV}, f = 495\text{mm},$
 $m = 10x)$

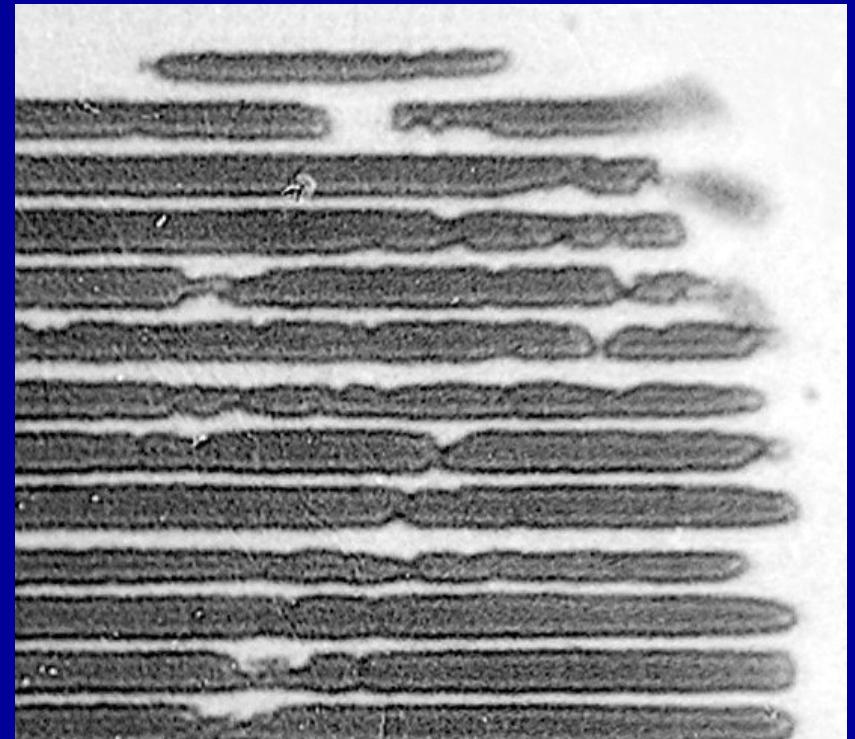
Lateral Resolution

Demonstration of resolution:
magnified image:



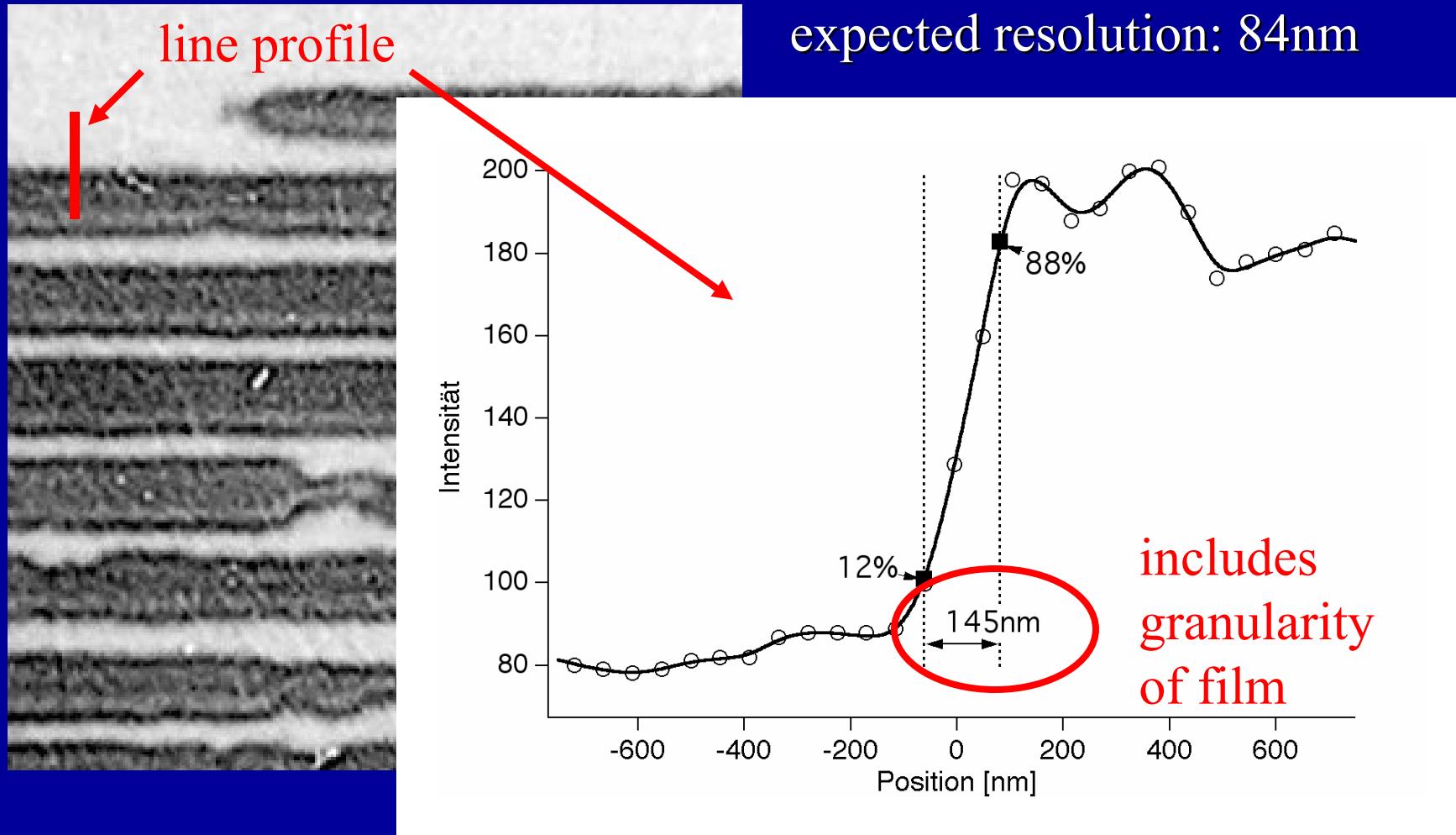
Al objective lens ($N = 120$)
($E = 25.5\text{keV}, f = 1.05\text{m}$,
 $m = 21\text{x}$)

magnified image:



Be objective lens ($N = 91$)
($E = 12\text{keV}, f = 495\text{mm}$,
 $m = 10\text{x}$)

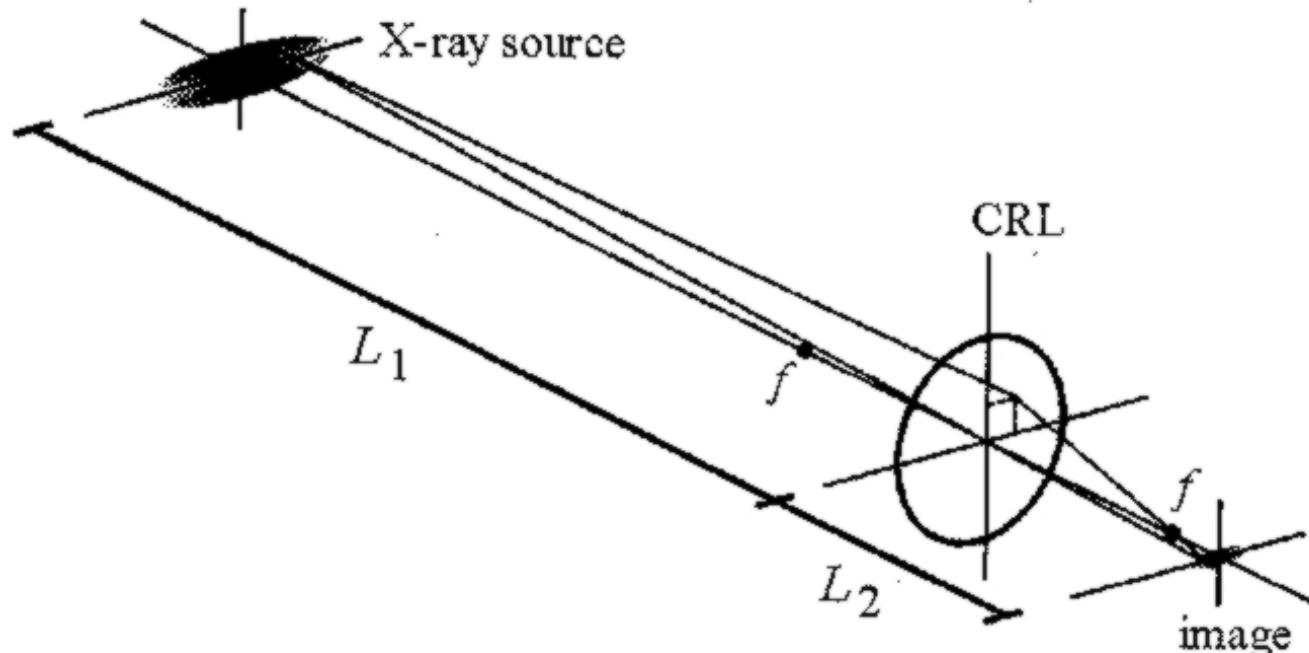
Lateral Resolution



→ deconvolution: optical resolution: $105\text{nm} \pm 30\text{nm}$ 25

C. MICROBEAM GENERATED BY PARABOLIC Be LENSES

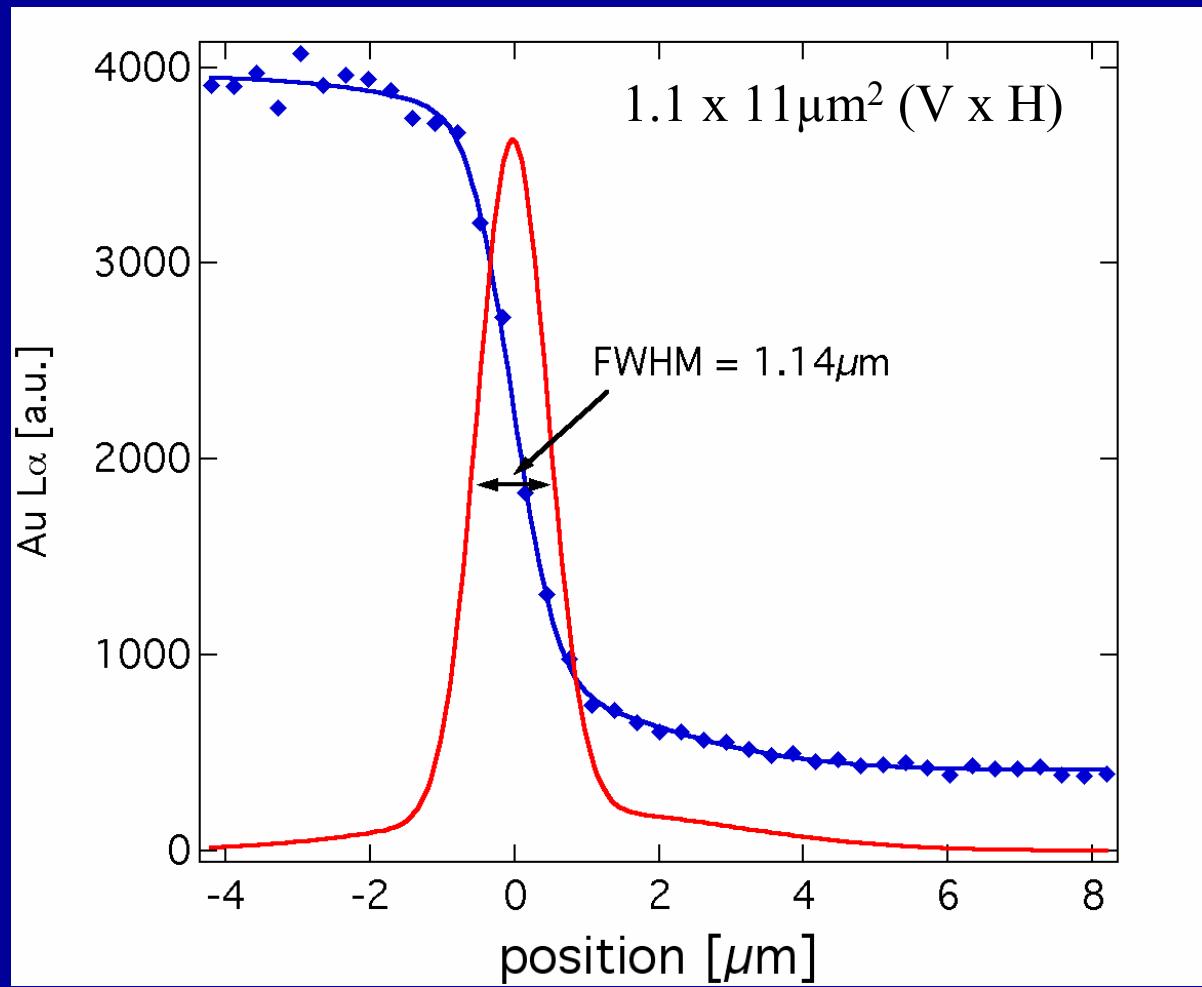
- parabolic lens images synchrotron radiation source onto sample



- x-ray microanalysis
 - diffraction choose $L_2 \ll L_1$ for small image !
 - fluorescence
 - absorption, small angle scattering

Microbeam ESRF ID22

Be lens ($N = 91$), $E = 12\text{keV}$, $L_1 = 41\text{m}$, $L_2 = 500\text{mm}$



flux in $1 \times 1\text{mm}^2$:
 $I_0 = 3.05 \cdot 10^{12} \text{ ph/s}$

flux behind lens:
 $I_{\text{tr}} = 1.05 \cdot 10^{11} \text{ ph/s}$

lens cross-section:
 0.024 mm^2
→ $d = 170\mu\text{m}$

equivalent to ideal
phase ZP with
275 μm aperture.

- in the meantime $d = 50\mu\text{m}$ is standard
- focal spot still limited by laws of geometrical optics
 - i.e. by source size, by source to lens distance and by focal length
- ESRF undulator: source size $20\mu\text{m}$ FWHM in vertical
 - $\Rightarrow 100$ to 200nm focal size to be expected,
 - in reality often (much) larger due to jitter in mirrors, monochromator.

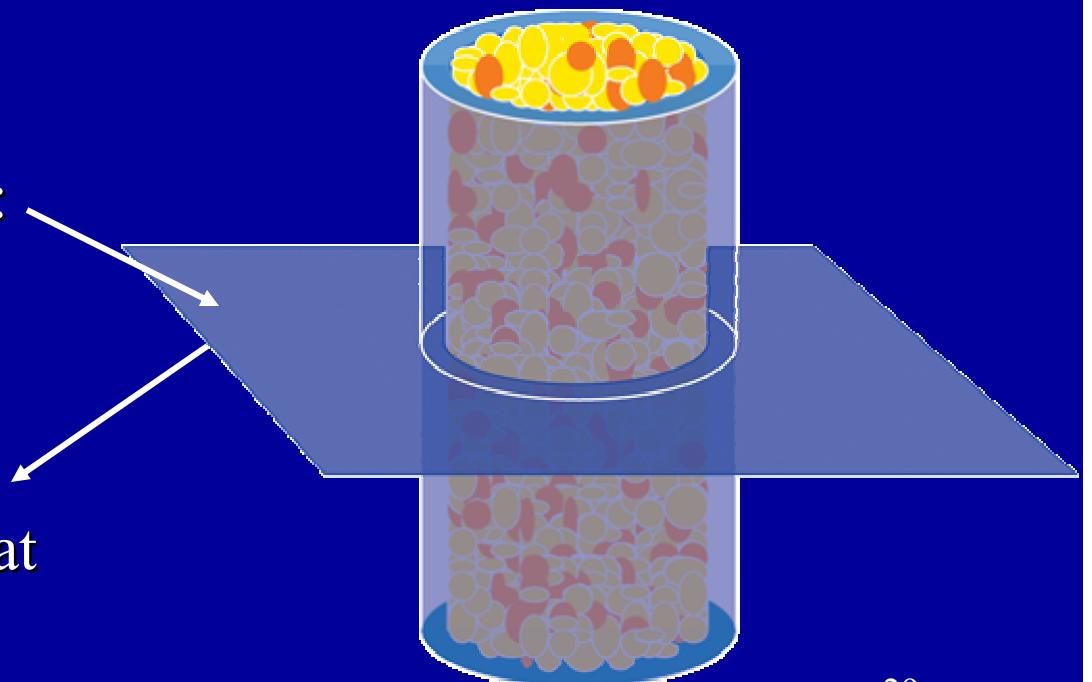
XANES Microtomography

Probe chemical state of a given element on a virtual section through the sample

nondestructive probe to the interior of sample

Sample:
CuO/ZnO catalyst + BN powder
in glass capillary

virtual slice through sample:

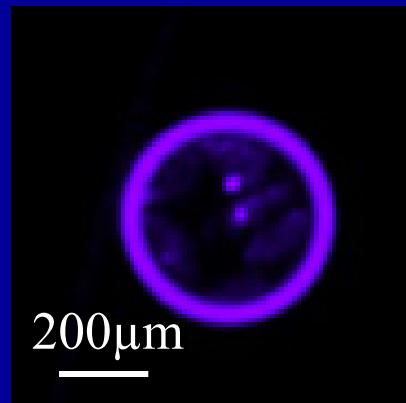


obtain absorption spectrum at each point of reconstruction

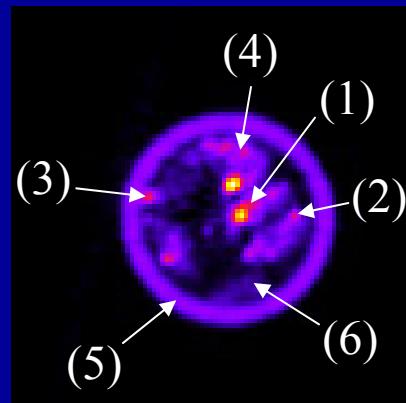
Reconstruction

At each energy: Standard filtered backprojection

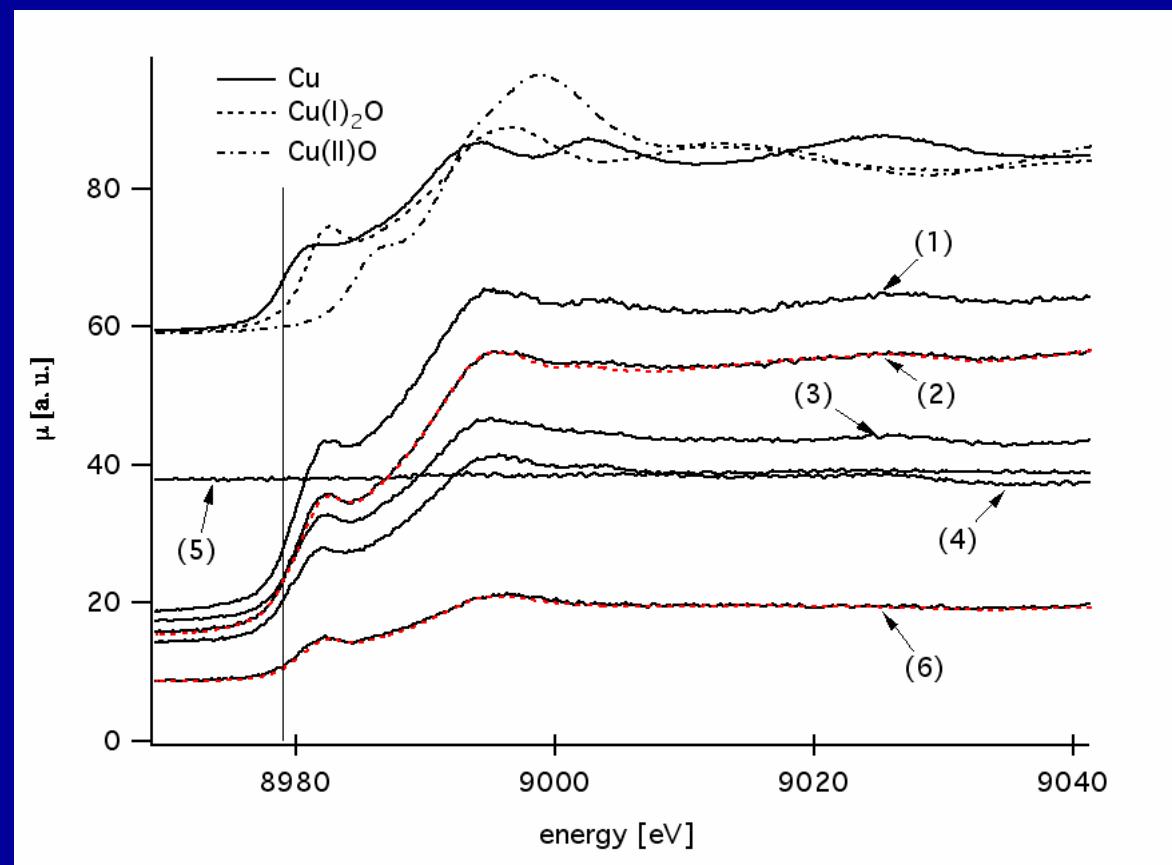
below Cu K-edge



above Cu K-edge

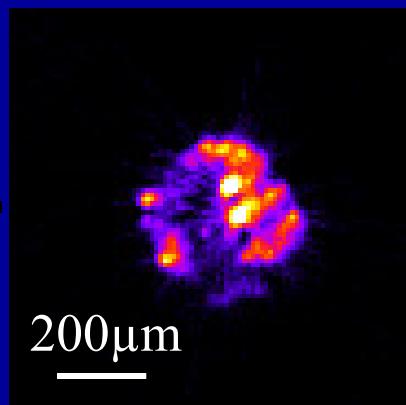


Reconstructed and reference spectra

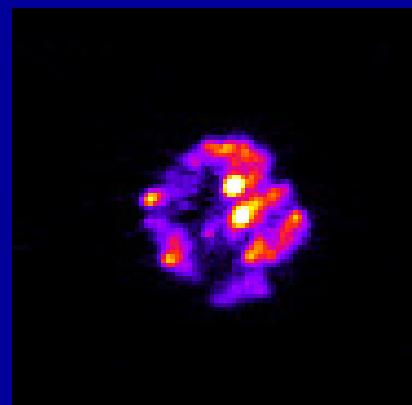


Distribution of Chemical Compounds

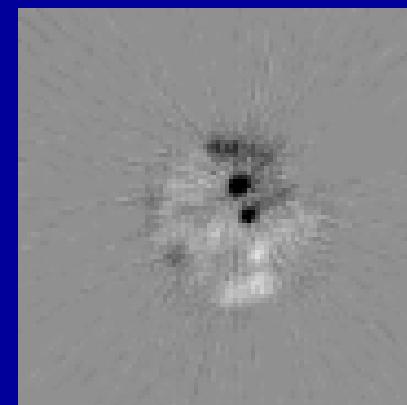
Cu (metallic)



$\text{Cu(I)}_2\text{O}$



difference

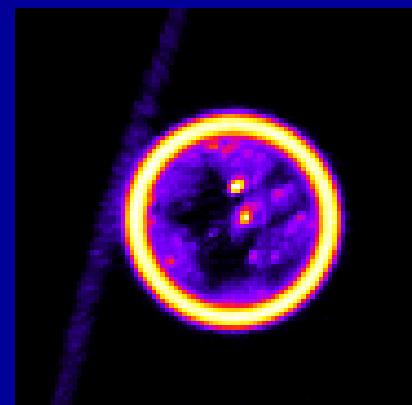


- + =

$\text{Cu(II)}\text{O}$



other elements



μ [a.u.]

see poster 10.22 tomorrow

Summary

- refractive lenses are excellent optical components for 5 to 120 keV, robust, stable in beam, easy to align and to operate, tunable
- well suited for imaging
 - no spherical aberration
 - large field of view
 - lateral resolution: reached 100 nm, expected 50 nm
 - limited by Compton scattering: 10 to 20 nm
- well suited for microfocus applications
 - focus limited by geometrical optics
 - large depth of field => tomography
- improvement: better quality Be with less small angle scattering! ³²